

Show that the length of the perimeter of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ ,  $a > b$  is  $4aE(e)$  where  $E(k) = \int_0^{\frac{\pi}{2}} \sqrt{1 - k^2 \cos^2 \theta} d\theta$  is the elliptic integral of the second kind and  $e = \sqrt{1 - \frac{b^2}{a^2}}$  is the eccentricity of the ellipse.