Let $f(x)=4 \sin ^{2}\left(\frac{\pi x}{12}\right)$ and $p_{n}(x)$ be its $n$th degree Lagrange polynomial on $[0,6]$ for equispaced points. Find $n$ such that $\left|f(x)-p_{n}(x)\right|<10^{-6}$.

